## Glossary of musical and mathematical terms

## Glossary of musical terms

| accent | Accented notes should be played with emphasis and a short attack. |
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| additive rhythm | An additive rhythm is one which is formed by combining small metrical <br> units. It moves from one note ( $\boldsymbol{x}$ time units long) to another note $(\boldsymbol{y}$ time <br> units long) where the sum of $\boldsymbol{x}$ plus $\boldsymbol{y}$ forms the metrical pattern such as 2 <br> $+3+4$ beats. |
| arpeggio | A type of broken chord in which the notes are played in order from the <br> lowest to the highest or vice versa. |
| atonality | The absence of key or tonal centre. |
| augmentation | A rhythmic device where note values are made longer, often doubled. |
| bars and barlines | Music is divided up into bars (sometimes known as measures) that contain <br> a specified number of beats. The bars are separated by barlines. |
| beat | The underlying pulse. |
| bpm | Beats per minute |
| cadence | Cadences are used to punctuate music, either bringing a melody to a point <br> of repose before going on, or bringing it to a close. Cadences are found at <br> the end of musical phrases and are usually harmonised by two chords. |
| canon | A canon is based on the principle of strict imitation, in which an initial <br> melody is imitated at a specified time interval by one or more parts. If <br> the imitation is exact and continues through the whole piece, the piece is <br> called a canon. A section of a piece is described as canonic if the imitation <br> prevails throughout the section |
| cantata | An extended piece of music for voices and accompaniment. |


| cantus firmus | A Latin term referring to a pre-existing melody used as the basis of a new <br> polyphonic composition. It is found mostly in Medieval and Renaissance <br> music. |
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| celesta | A small keyboard instrument with an ethereal bell-like sound. |
| chord | The simultaneous sounding of two or more notes to produce harmony. |
| chord progression <br> or chord sequence | A repeated sequence of chords. |
| chorus | A setting of the refrain of the lyrics. The chorus usually returns several <br> times, and, in popular music, is likely to be the catchiest part of the song. |
| chromatic | Chromatic notes are those outside the prevailing major or minor key. |
| chromatic <br> harmony | Chromatic harmony uses notes from outside the prevailing key to colour <br> the chords |
| chromatic scale | A scale made up of all the twelve notes in an octave and formed entirely of <br> semitones. |
| circle of fffths |  |
| (cycle of fifths) | The circle of 5ths is represented by a circular diagram demonstrating the <br> relationship between different keys. It shows a series of chords whose <br> roots are each a 5th higher than the previous chord e.g. C-G-D-A. From <br> any starting note the pitch is raised repeatedly until the starting point is <br> returned to. |
| diatonic scale | A concluding section. |
| coda | Where specific instruments (such as gongs) mark the beginnings and ends <br> of rhythmic cycles. |
| colotomic <br> structure | scales. Diatonic scales have seven notes. Major scales include five steps of a <br> tone and two steps of a semitone. |
| A technique found in twelve-note compositions whereby a collection of |  |
| pitch classes can be combined with a transformation of itself to form an |  |
| aggregate of all 12 pitch classes. |  |$|$| This refers to the commonly-used time signature of 4/4 and is denoted by |
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| the sign C at the beginning of a piece. |


| diminution | A rhythmic device where note values are made shorter, often halved. |
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| dissonance | Dissonant chords feel somewhat unstable or discordant. |
| divisive rhythm | A divisive rhythm system uses regularly repeated units (bars or measures) <br> which can be divided into smaller parts (usually two, three or four beats). |
| dodecaphony | See serialism |
| dominant seventh | Dominant 7th chords are built on the fifth degree of the scale (the <br> dominant). They are made up of four notes: the first, third and fifth notes <br> of a given scale - plus a flattened 7th note from that scale. |
| drone | The extended sustaining or repetition of a note. |
| dynamics | The dynamics of a piece indicate the variations in loudness between notes <br> or phrases. |
| enharmonic <br> equivalent | Notes that sound the same but are written (or spelt') differently are said to <br> be enharmonic e.g. E\# and F where E\# is the enharmonic equivalent of F |
| ensemble | A group of soloists, singers or instrumentalists, performing together. |
| figures or <br> figuration | Short repeated patterns of notes with a distinctive shape (e.g. scales or <br> arpeggio patterns), often used as decoration or accompaniment. |
| flat | A flat (b) placed before a note lowers its pitch by one semitone. |
| forte/fortissimo | Loud/very loud |
| four-on-the-floor | A rhythmic pattern where the bass drum accents each of the four beats in <br> a 4/4 bar. Often found in disco music. |
| fugal | A contrapuntal style using a good deal of imitation. |
| functional |  |
| harmony | A contrapuntal musical form which follows a detailed set of rules: two or <br> more voices use the systematic imitation of a principal theme (the subject) <br> an answer and (sometimes) a countersubject in simultaneously sounding <br> melodic lines (counterpoint). |
| fugue |  |
| music, and the visual arts, often within a loose structure and without a |  |
| plot. |  |


| harmony | Harmony is produced when any combination of notes are sounded <br> together. |
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| hemiola | A pattern that occurs when three beats are performed in the time of two <br> or two beats are performed in the time of three. |
| hexachord | A six note pattern. |
| imitation | Imitation occurs when an initial melody (or rhythm) is imitated at a <br> specified time interval by one or more parts. |
| improvisation | A performance where the music (or part of it) is made up on the spot. |
| instrumentation | The particular instruments used in a piece of music. |
| integral serialism | See total serialism. |
| interval | The distance between two notes. |
| intro | The opening section of a song. |
| isorhythm | A rhythmic technique using multiple repetitions of the same rhythm <br> against different pitch patterns. |
| key | When a piece of music is based on a particular scale it is said to be in the <br> key of that scale. |
| key signature | A sign at the beginning of each stave of music indicating the key of the <br> piece. |
| loops and looping | Where a short section or sample, often rhythmic in nature, is constantly <br> repeated. |
| metre | The organisation of regular pulses into patterns of strong and weak beats. |
| metric |  |
| modulation | Where there is a change in pulse rate or time signature wherein a note <br> value from the first section is made equivalent to a note value in the second <br> section. |
| microtone | An interval smaller than a semitone. |
| modes of limited |  |
| transposition | A term first used by the French composer Olivier Messiaen to denote <br> scales which can be transposed a limited number of times before the <br> original set of pitches reappears. Examples include the whole tone scale <br> and the octatonic scale. |
| modulation | The change from one key to another. |
| motif | A short melodic or rhythmic idea. |


| note row | Note rows (also known as tone rows) form the basis of serialism. A note <br> row uses all 12 notes of the chromatic scale and is the basis of the whole <br> composition. There are four main permutations of the row. They are <br> often referred to as the prime order, inversion, retrograde and retrograde <br> inversion. |
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| octatonic scale | The octatonic scale is made up of eight notes alternating tones and <br> semitones |
| octave | The interval between the first and last notes of a major or minor scale. The <br> two notes have the same letter name. |
| oral tradition | Where music is transmitted from one generation to another by word of <br> mouth. |
| orchestration | The scoring of instruments used in an arrangement. |
| ostinato | A short musical pattern repeated throughout a section or complete piece. <br> The plural is ostinati. |
| pentatonic scale | Pentatonic scales are made up of five notes. There are several different <br> versions. They can be categorized as either hemitonic (with semitones) or <br> anhemitonic (without semitones). |
| phase shifting or | Where one part repeats constantly and another gradually shifts out of <br> phase with it. |
| phrase | A subdivision of a melodic line. |
| piano/pianissimo | Quiet/very quiet |
| pitch | The word used to describe how high or low a sound is. |
| pizzicato | A string technique where the instrument is plucked with the fingers. |
| polymetric | Where different meters are combined simultaneously. |
| polyphony | A style of music that combines several distinct melodic lines <br> simultaneously. |
| prise distance between the lowest and highest notes of a melody or |  |
| composition. |  |


| register | A particular part of the range of a voice (e.g. chest or head voice) or instrument (e.g. high or low register). |
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| retrograde | Where an existing melody or rhythm is played backwards. |
| rhythmic serialism | Where the principles of serialism are applied to rhythm. |
| riff | A short, repeated melodic or chordal pattern that may be heard at different pitches to fit in with the harmony. |
| sample | A recorded fragment of sound, newly recorded or from a pre-existing source. |
| scale | A pattern of notes arranged in order from low to high (or vice versa). |
| score | The written form of a musical composition. |
| semitone | A semitone is a measurement of pitch. There are semitones between all adjacent notes on a keyboard, whether black or white. |
| septuple rhythm | Where rhythms are divided into seven beats e.g. $3+4$ or $4+3$. |
| serialism <br> (dodecaphony or <br> 12-note system) | The twelve-note system of serialism (sometimes known as dodecaphony) follows strict mathematical rules in the form of an algorithm. First of all a note row (or series) is composed that is the basis of the whole composition. There are four main permutations of the row - often referred to as the prime order, inversion, retrograde and retrograde inversion. |
| set theory | In music a set is a group of pitch classes, usually a 12 -note set, it may also be a set of other musical elements such as durations or dynamics. Music set theory categorises musical objects and analyses their relationships. |
| sharp | A sharp (\#) placed before a note raises its pitch by one semitone |
| slendro | A five-note scale used in Javanese gamelan music. |
| solmization | A sight-singing system where a set of syllables is matched to the degrees of the scale - ut, re, mi, fa, sol, la. |
| song cycle | A group of songs designed to be performed together as one unit. |
| sruti | A microtonal interval used in Indian music. |
| syncopation | The effect created when off-beat notes are accented |
| tala | A repeated cyclical rhythm pattern used in Indian music. |
| tempo | The speed of a piece of music. |
| texture | The number of parts in a piece of music and how they relate to one another. The texture of a piece refers to the overall picture of the sound. |
| timbre | Tone colour. The characteristic quality of a musical sound. |


| time line | A short repeated rhythm which is either clapped or played by a single or <br> double bell. |
| :--- | :--- |
| time signature | A numerical sign found at the beginning of a piece of music telling you the <br> number of beats in each bar and the note-value of the beat. |
| tonal ambiguity | This occurs when it is not clear what key a passage is in. |
| tonal harmony | Where the harmony is centred on diatonic keys. |
| tonality | The key centre or mode of a piece of music. |
| tone colour | Timbre. The characteristic quality of a musical sound. |
| total serialism <br> (integral <br> serialism) | Where the procedures of serialism are extended to the other aspects of the <br> music beyond pitch, such as rhythm, dynamics, tempo, timbre and note <br> attack. |
| transposition | Where a passage of music is written or performed at a different pitch. |
| triple time | Three beats in a bar. |
| triplet | Where three notes are played in the time of two. |
| twelve-note <br> system | See serialism. |
| unison | Two voices producing the same pitch are said to be in unison. |
| verse and chorus | A standard song form where the verse and chorus usually alternate. The <br> verses have the same or similar music but different text. The choruses <br> usually repeat the same words and music. |
| whole tone scale | The whole tone scale is made up of six whole tones starting on either C or <br> Db (its only transposition). |

## Glossary of mathematical terms

| $\mathbf{1 / f}$ distribution | In terms of noise, $1 f$ noise (or fractal noise) is a signal with a frequency <br> spectrum such that the power per frequency interval is inversely <br> proportional to the frequency (symbol $f$ ) of the signal. |
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| $\mathbf{1 8 0}^{\circ}$ rotation | A function that moves each point of the plane through an angle of $180^{\circ}$ <br> about a fixed point. |
| $p b i-\Phi$ | The Greek letter $p h i-\Phi$, an irrational number, is used to denote the value <br> of the golden ratio. |


| algorithm | Where a set of precisely described instructions or routine procedures are designed to be applied systematically through to a conclusion in a number of steps. |
| :---: | :---: |
| Brownian motion | A continuous-time version of the random walk displayed by minute particles of solid matter when suspended in a fluid or a gas resulting from their collision with the fast-moving molecules in the fluid. |
| Butterfly Effect | The way a small change in one state of a deterministic system can bring about large differences in a later state with the potential to render long-term predictions impossible. |
| Cantor set | The Cantor set, sometimes known as the middle third Cantor set, is obtained by repeatedly removing the middle thirds of intervals. Each stage of the construction is obtained by removing the middle third of the previous stage. |
| cent | A logarithmic unit of measurement for the ratio between two frequencies. |
| chaos theory | Chaos theory (the science of dynamical systems) focuses on the behaviour occurring in a system under iteration and is the study of apparently random or unpredictable behaviour in systems governed by deterministic laws. |
| cipher | A cipher uses an algorithm, which usually replaces a letter or other single character with another, to convert the plaintext, a message, for example, into another text known as the ciphertext. |
| coding | Coding theory refers to the reliable transmission of data and to the detection of and correction of errors in its transmission. |
| combinatorics | The study of the enumeration, combination and permutation of sets of elements and the mathematical characteristics of their properties. |
| cryptogram | An enciphered message written in code. The original message is called the plaintext and the enciphered message is called the cryptogram. |
| cryptography | The practice of writing in code or cipher aiming to conceal information. |
| deterministic system | A system in which no randomness is involved in the development of future states of the system. If the initial state is known exactly then the future state could, in theory, be predicted. A model which incorporates random elements or processes is said to be stochastic, otherwise it is said to be a deterministic model. |
| devil's staircase | In mathematics a devil's staircase (sometimes referred to as the infinite staircase or the Cantor function) has unequal ascending steps constructed by using, for example the recursive $1 / 3$ to $2 / 3$ proportions of the most common middle-thirds Cantor set. |
| dynamical system | A dynamical system is a mathematical system whose state is uniquely specified by a set of variables and whose behaviour is described by predefined rules. |
| encryption | The process of converting the plaintext to ciphertext is called encryption, with decryption denoting the reverse process. |


| Euclidean algorithm | The Euclidean algorithm is a systematic repetitive procedure used for computing the greatest common divisor (GCD) of two integers. |
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| Euclidean rhythm | In the Euclidean rhythm $E(k, n), k$ is the number of ones (onsets), and $n$ (the number of pulses) is the length of the sequence (zeroes plus ones). |
| Fibonacci series | A summation series in which each number is the sum of the two which precede it. |
| fractal | Fractals belong to a class of curves or complex geometric shapes where each part has the same statistical character as the whole, that is, it is made up of smaller scale copies of itself. |
| frequency | Frequency $(f)$ is the number of occurrences of a repeating event per unit of time. Frequency is measured in hertz $(\mathrm{Hz})$. A hertz is equal to one event per second. For cyclical phenomena such as sound waves frequency is defined as the number of cycles or repetitions per unit of time. |
| frequency analysis | Part of descriptive statistics which measures the number of times an event occurs. |
| frieze pattern | A repeating pattern of elements arranged along a line or in a strip. |
| Gaussian distribution | Gaussian distribution (often known as normal distribution) is a very common continuous probability distribution and is the basis of a large proportion of statistical analysis. |
| GCD | See greatest common divisor. |
| glide | A form of symmetry where a figure is reflected and then translated by being shifted horizontally. |
| Golden Section | The unequal division of a line into two parts such that the ratio of the smaller part to the larger is the same as that of the larger to the original whole. This ratio is approximately 1:1618. |
| greatest common divisor (GCD) | The GCD of two or more numbers is the greatest common factor number that divides them exactly. |
| group theory | A branch of abstract algebra, which looks at the main features of a group, from both the point of view of its elements and its group operations. |
| infinite | Having a size or absolute value greater than any natural number (positive integer). |
| integer | A whole number (not a fraction) that can be positive, negative or zero. Positive integers are sometimes known as natural numbers. |
| invariance | A property or quantity is said to be invariant if it is not changed by one or more specified operations or transformations. |
| irrational number | A real number which cannot be expressed as an integer or as a quotient of two integers. Irrational numbers have infinite, non-repeating decimals. |
| iteration | A method uses iteration if it yields successive values by repetition of a certain procedure. |
| Latin square | A square array of symbols arranged in rows and columns such that each row or column of the array contains each symbol precisely once. |


| LCM | See least common multiple. |
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| least common multiple (LCM) | The LCM of two positive integers is the smallest integer that each number divides into evenly. |
| Lucas summation series | An integer sequence which has the same recursive relationship as the Fibonacci sequence, where each term is the sum of the two previous terms, but with different starting values. |
| magic square | A square matrix where a different positive integer is written in each cell, each occurs only once. The 'magical' quality is that each horizontal, vertical and diagonal row adds up to the same number. |
| Möbius strip | A 2-dimensional strip where one continuous side is formed by joining the ends of a rectangle after twisting one end through $180^{\circ}$. |
| modular <br> arithmetic | A system of arithmetic for integers which gives the remainders in division. |
| Moiré patterns | Geometrical designs produced when a set of straight or curved lines is superimposed onto another set. |
| multiplier | The number or term by which another is multiplied in multiplication. |
| $n$ factorial | The product of all positive integers less than or equal to $n$. |
| prime number | A number that can only be divided by itself and 1 without remainders. Numbers that are relatively prime have no common factors other than 1 . |
| probability | The probability of an event is a measurement of the possibility of the event occurring. |
| randomness | Having no specific pattern, purpose or principle of organization. |
| random numbers | Random numbers have two main properties: all of the numbers or digits in the numeric sequence will, in the long run, occur equally often; and the occurrence of any one number or digit in a particular position in the sequence is no guide to the occurrence of the number or digit later in the sequence. |
| random walk | A process in which a sequence of discrete steps of fixed length is described in terms of the movement of a particle, so in a one-dimensional random walk the state of the process is described as a position on a straight line. |
| ratio | The quotient of two numbers or quantities giving their relative size. The ratio of $x$ to $y$ is written as $x: y$ ( $\operatorname{or} x / y$ ) and is unchanged if both quantities are multiplied by the same quantity. |
| rational number | A rational number is one which is either an integer or can be written as a ratio (or quotient) of two integers e.g. 1, 7, 544 or 2/3. |
| recursive construction | Recursive construction involves repeating the same a simple step over and over again. |
| reflection | When an object has reflectional symmetry it can be divided into two pieces which are images of each other. The dividing line is known as the axis of symmetry. This could be the on the horizontal x axis (vertical reflection) or the vertical y axis (horizontal reflection). |


| rotation | When an object has rotational symmetry it can be turned about a fixed <br> point whilst keeping the same overall shape. |
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| Sator square | An ancient palindromic $5 \times 5$ Latin square using the letters S A T O R that <br> can be read horizontally, vertically and backwards. |
| scale symmetry | An object has scale symmetry when it can be expanded or contracted whilst <br> keeping the same overall shape. |
| self-similarity | A self-similar object is one whose component parts resemble the whole. |
| set theory | A set is a well-defined collection of objects which are referred to as elements <br> or members. Set theory is the study of the properties of sets and their <br> relations. |
| stochastic process | A process in which the steps are governed by rules of probability. Stochastic <br> processes are random and non-deterministic; the next state of the <br> environment is not fully determined by the previous one |
| summation series | An infinite sequence in which each number is the sum of the two which <br> precede it. |
| symmetry | A geometric object or shape is symmetric if it can be divided into two or <br> more identical parts and is invariant under transformation. There are several <br> different types of transformation; the main types are reflection, rotation, <br> translation, and scale. |
| translation | When an object has translational symmetry it can be shifted a fixed distance <br> in a fixed direction whilst keeping the same overall shape. This can happen <br> in two ways. It can be shifted from left to right - horizontal translation or It <br> can be shifted upwards or downwards - vertical translation. |
| variable | An expression, usually denoted by a letter that is defined for different values <br> within a given set. |
| xoaxis Koch curve | A fractal curve, the main von Koch curve contains many tiny von Koch <br> curves which are made up of smaller scale copies of itself. This property is <br> known as self-similarity. |
| y-axis | The von Koch snowflake is developed from the von Koch curve. Instead <br> of one line the snowflake begins with an equilateral triangle. The steps in <br> creating the Koch curve are then repeatedly applied to each side of the <br> equilateral triangle, creating a snowflaké shape. |
| von Koch |  |
| snowflake | The horizontal axis of a graph. |
| The vertical axis of a graph |  |

